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**Started on** Sunday, 10 January 2021, 9:46 AM

**State** Finished

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**Time taken** 1 hour 15 mins

**Grade** 25.00 out of 32.00 (78%)

**Question 1**

Correct

Mark 1.00 out of 1.00

If  $\{v_1, v_2, v_3, v_4\}$  is a basis for a vector space  $V$ , then the set  $\{v_1, v_2, v_3\}$  is

Select one:

- a. linearly dependent and not a spanning set for  $V$ .
- b. linearly independent and not a spanning set for  $V$ .  
✓
- c. linearly independent and a spanning set for  $V$ .
- d. linearly dependent and a spanning set

The correct answer is: linearly independent and not a spanning set for  $V$ .

**Question 2**

Correct

Mark 1.00 out of 1.00

If  $A$  is a  $3 \times 5$ -matrix, rows of  $A$  are linearly independent, then

Select one:

- a.  $\text{rank}(A) = \text{nullity}(A) + 2$
- b.  $\text{rank}(A) = \text{nullity}(A)$
- c.  $\text{rank}(A) = \text{nullity}(A) + 3$
- d.  $\text{rank}(A) = \text{nullity}(A) + 1$   
✓

The correct answer is:  $\text{rank}(A) = \text{nullity}(A) + 1$

**Question 3**

Correct

Mark 1.00 out of 1.00

If  $A$  is a  $3 \times 2$  matrix, then

Select one:

- a. The columns of  $A$  are linearly independent
- b. The rows of  $A$  are linearly dependent  
✓
- c.  $\text{Rank}(A) = 3$
- d. The columns of  $A$  are linearly dependent

The correct answer is: The rows of  $A$  are linearly dependent

**Question 4**

Incorrect

Mark 0.00 out of 1.00

The coordinate vector of  $6 + 4x$  with respect to the basis  $[2x, 2]$  is  $(3, 2)^T$

Select one:

- a. True ✗
- b. False

The correct answer is: False

**Question 5**

Correct

Mark 1.00 out of 1.00

The rank of  $A = \begin{pmatrix} 1 & 4 & 1 & 2 & 2 \\ 2 & 6 & -1 & 2 & 1 \\ 3 & 10 & 0 & 4 & 3 \end{pmatrix}$  is

Select one:

- a. 3
- b. 1
- c. 2 ✓
- d. 4

The correct answer is: 2

**Question 6**

Correct

Mark 1.00 out of 1.00

If  $A = \begin{pmatrix} -1 & -2 & -1 & 0 \\ 1 & 2 & 2 & 0 \\ -2 & -4 & 0 & 0 \end{pmatrix}$ , then  $\text{rank}(A) = 3$ .

Select one:

- a. True
- b. False ✓

The correct answer is: False

**Question 7**

Correct

Mark 1.00 out of 1.00

The vectors  $\{-x + 1, 2x^2 + 3x + 3, x^2 + x + 2\}$  form a basis for  $P_3$ .

Select one:

- a. False ✓
- b. True

The correct answer is: False

**Question 8**

Correct

Mark 1.00 out of 1.00

Let  $V$  be a vector space,  $v_1, v_2, \dots, v_n \in V$  be linearly independent, and  $v \in V$ , then the vectors  $v_1, v_2, \dots, v_n, v$  are linearly independent.

Select one:

- a. True
- b. False ✓

The correct answer is: False

## Question 9

Correct

Mark 1.00 out of 1.00

dimension of the subspace  $S = \text{Span} \left\{ A_1 = \begin{pmatrix} 0 & 1 \\ 2 & 1 \end{pmatrix}, A_2 = \begin{pmatrix} 3 & 1 \\ -1 & 0 \end{pmatrix}, A_3 = \begin{pmatrix} 6 & -1 \\ -8 & -3 \end{pmatrix} \right\}$  is

Select one:

- a. 1
- b. 3
- c. 2
- d. 0

The correct answer is: 2

## Question 10

Incorrect

Mark 0.00 out of 1.00

If  $T_{n \times n}$  is a transition matrix between two bases for a vector space  $V$ ,  $\dim(V) = n > 0$ , then

Select one:

- a.  $\text{rank}(T) = 1$
- b.  $\det(T) = 1$
- c.  $\text{nullity}(T) = n$
- d.  $T$  is nonsingular

The correct answer is:  $T$  is nonsingular

## Question 11

Correct

Mark 1.00 out of 1.00

Let  $S = \{f \in C[-1, 1] : f(-1) = f(1)\}$ , then  $S$  is a subspace of  $C[-1, 1]$ .

Select one:

- a. True
- b. False

The correct answer is: True

## Question 12

Correct

Mark 1.00 out of 1.00

Let  $A$  be a  $4 \times 6$  matrix, and  $\text{nullity}(A) = 2$ , then the system  $Ax = b$  has infinite number of solutions for every  $b \in \mathbb{R}^4$ .

Select one:

- a. True
- b. False

The correct answer is: True

## Question 13

Correct

Mark 1.00 out of 1.00

Let  $S = \left\{ \begin{pmatrix} x \\ y \end{pmatrix} \in \mathbb{R}^2 : x = 1 - y \right\}$ , then  $S$  is a subspace of  $\mathbb{R}^2$ .

Select one:

- a. True
- b. False

The correct answer is: False

## Question 14

Correct

Mark 1.00 out of 1.00

$\dim(\text{span}(x^2, 3 + x^2, x^2 + 1))$  is

Select one:

- a. 1
- b. 0
- c. 3
- d. 2



The correct answer is: 2

## Question 15

Correct

Mark 1.00 out of 1.00

If  $v_1, v_2, \dots, v_n \in V$ ,  $\dim(V) = n$  and  $v_1, v_2, \dots, v_n$  are linearly independent, then  $\text{Span}(v_1, v_2, \dots, v_n) = V$ .

Select one:

- a. False
- b. True



The correct answer is: True

## Question 16

Correct

Mark 1.00 out of 1.00

let  $A$  be a  $3 \times 5$ -matrix, if the row echelon form of  $A$  has 1 nonzero row, then  $\dim(\text{column space of } A)$  is

Select one:

- a. 2
- b. 0
- c. 3
- d. 1



The correct answer is: 1

## Question 17

Incorrect

Mark 0.00 out of 1.00

If  $f_1, f_2, \dots, f_n \in C^{n-1}[a, b]$  and  $W[f_1, f_2, \dots, f_n](x_0) = 0$  for some  $x_0 \in [a, b]$ , then  $f_1, f_2, \dots, f_n$  are linearly dependent.

Select one:

- a. False
- b. True



The correct answer is: False

## Question 18

Incorrect

Mark 0.00 out of 1.00

Let  $E = [3 - x, 2 + x]$ ,  $F = [1, x]$  be ordered bases for  $P_2$ . The transition matrix from  $E$  to  $F$  is

Select one:

- a.  $\begin{pmatrix} -1 & 1 \\ 3 & 2 \end{pmatrix}$
- b.  $\begin{pmatrix} 1 & 2 \\ -1 & 3 \end{pmatrix}$
- c.  $\begin{pmatrix} -1 & 1 \\ 2 & 3 \end{pmatrix}$
- d.  $\begin{pmatrix} 3 & 2 \\ -1 & 1 \end{pmatrix}$

The correct answer is:  $\begin{pmatrix} 3 & 2 \\ -1 & 1 \end{pmatrix}$

## Question 19

Correct

Mark 1.00 out of 1.00

Let  $E = [2 + x, 1 - x, x^2 + 1]$  be an ordered basis for  $P_3$ . If  $p(x) = -3x^2 + x + 5$ , then the coordinate vector of  $p(x)$  with respect to  $E$  is

Select one:

- a.  $\begin{pmatrix} 3 \\ -3 \\ 2 \end{pmatrix}$
- b.  $\begin{pmatrix} 3 \\ 5 \\ 4 \end{pmatrix}$
- c.  $\begin{pmatrix} 2 \\ -3 \\ 3 \end{pmatrix}$
- d.  $\begin{pmatrix} 3 \\ 2 \\ -3 \end{pmatrix}$

The correct answer is:  $\begin{pmatrix} 3 \\ 2 \\ -3 \end{pmatrix}$

## Question 20

Incorrect

Mark 0.00 out of 1.00

The transition matrix from the standard basis  $S = \left[ e_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, e_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right]$  to the ordered basis  $U = \left[ u_1 = \begin{pmatrix} 2 \\ 3 \end{pmatrix}, u_2 = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \right]$  is

Select one:

a.  $T = \begin{pmatrix} 2 & -1 \\ -3 & 2 \end{pmatrix}$

b.  $T = \begin{pmatrix} 2 & 3 \\ 1 & 2 \end{pmatrix}$

c.  $T = \begin{pmatrix} 2 & 1 \\ 3 & 2 \end{pmatrix}$

✘

d.  $T = \begin{pmatrix} -2 & 1 \\ 3 & -2 \end{pmatrix}$

The correct answer is:  $T = \begin{pmatrix} 2 & -1 \\ -3 & 2 \end{pmatrix}$

## Question 21

Correct

Mark 1.00 out of 1.00

The coordinate vector of  $\begin{pmatrix} -3 \\ -2 \\ -5 \end{pmatrix}$  with respect to the ordered basis  $\left[ \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 2 \\ 2 \end{pmatrix}, \begin{pmatrix} 2 \\ 3 \\ 4 \end{pmatrix} \right]$  is

Select one:

a.  $\begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$

b.  $\begin{pmatrix} 3 \\ 2 \\ 5 \end{pmatrix}$

c.  $\begin{pmatrix} 1 \\ -4 \\ 3 \end{pmatrix}$

d.  $\begin{pmatrix} -1 \\ 4 \\ -3 \end{pmatrix}$

✔

The correct answer is:  $\begin{pmatrix} -1 \\ 4 \\ -3 \end{pmatrix}$

## Question 22

Correct

Mark 1.00 out of 1.00

If two nonzero vectors in a vector space  $V$  are linearly dependent, then each of them is a scalar multiple of the other.

Select one:

a. True ✔

b. False

The correct answer is: True

## Question 23

Incorrect

Mark 0.00 out of 1.00

Which of the following **is not a basis** for the corresponding space

Select one:

- a.  $\{x + 4, 1 - x^2, x^2 + x + 3\}; P_3$   
✘
- b.  $\{(1, 1)^T, (2, -3)^T\}; \mathbb{R}^2$
- c.  $\{5 - x, x - 1\}; P_2$
- d.  $\{(-2, -1, -1)^T, (-3, -3, 0)^T, (2, 0, 2)^T\}; \mathbb{R}^3$

The correct answer is:  $\{(-2, -1, -1)^T, (-3, -3, 0)^T, (2, 0, 2)^T\}; \mathbb{R}^3$ 

## Question 24

Correct

Mark 1.00 out of 1.00

If  $v_1, v_2, \dots, v_k$  are vectors in a vector space  $V$ , and  $\text{Span}(v_1, v_2, \dots, v_k) = \text{Span}(v_1, v_2, \dots, v_{k-1})$ , then  $v_k$  can be written as a linear combination of  $v_1, v_2, \dots, v_{k-1}$

Select one:

- a. True ✔
- b. False

The correct answer is: True

## Question 25

Correct

Mark 1.00 out of 1.00

If  $A$  is an  $m \times n$ -matrix, and columns of  $A$  are linearly independent, then

Select one:

- a.  $m = n$
- b.  $m = n + 1$
- c.  $m \leq n$
- d.  $n \leq m$   
✔

The correct answer is:  $n \leq m$ 

## Question 26

Correct

Mark 1.00 out of 1.00

Let  $A$  be a  $5 \times 4$  matrix, and  $\text{rank}(A) = 4$ 

Select one:

- a.  $A$  has a row of zeros
- b. The columns of  $A$  are linearly independent  
✔
- c.  $\text{nullity}(A) = 1$
- d. The rows of  $A$  are linearly independent

The correct answer is: The columns of  $A$  are linearly independent

## Question 27

Incorrect

Mark 0.00 out of 1.00

If  $A$  is a nonzero  $4 \times 2$ -matrix and  $Ax = 0$  has infinitely many solutions, then  $\text{rank}(A) =$

Select one:

- a. 2  
✘
- b. 4
- c. 3
- d. 1

The correct answer is: 1

## Question 28

Correct

Mark 1.00 out of 1.00

If  $A$  is a  $4 \times 3$  matrix with  $\text{rank}(A) = 3$ , then the homogeneous system  $Ax = 0$  has a nontrivial solution.

Select one:

- a. False ✔
- b. True

The correct answer is: False

## Question 29

Correct

Mark 1.00 out of 1.00

let  $A$  be a  $4 \times 7$ -matrix, if the row echelon form of  $A$  has 2 nonzero rows, then  $\dim(\text{column space of } A)$  is

Select one:

- a. 7
- b. 5
- c. 2 ✔
- d. 3

The correct answer is: 2

## Question 30

Correct

Mark 1.00 out of 1.00

The functions  $\sin x, \cos x, \sin(2x)$  in  $C^2[0, 2\pi]$  are

Select one:

- a. linearly dependent
- b. linearly independent ✔

The correct answer is: linearly independent

## Question 31

Correct

Mark 1.00 out of 1.00

If  $A$  is a  $3 \times 3$ -matrix, and  $Ax = 0$  has only the zero solution, then  $\text{nullity}(A) =$

Select one:

- a. 1
- b. 3
- c. 2
- d. 0 ✔

The correct answer is: 0



## Question 32

Correct

Mark 1.00 out  
of 1.00

The vectors  $\{(1, -1, -4)^T, (1, -1, 1)^T, (1, -1, 2)^T\}$  form a basis for  $\mathbb{R}^3$ .

Select one:

- a. False ✓
- b. True

The correct answer is: False

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